

Chapter 1 : Design and Analysis of Computer Algorithms

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Recursive algorithms An algorithm is said to be recursive if the same algorithm is invoked in the body direct recursive. Algorithm A is said to be indirect recursive if it calls another algorithm which in turn calls A. Factorial computation $n!$ Binomial coefficient computation Example 3: Tower of Hanoi problem Example 4: Analysis Framework General framework for analyzing the efficiency of algorithms is discussed here. There are two kinds of efficiency: Time efficiency indicates how fast an algorithm in question runs; space efficiency deals with the extra space the algorithm requires. In the early days of electronic computing, both resources time and space were at a premium. Now the amount of extra space required by an algorithm is typically not of as much concern. In addition, the research experience has shown that for most problems, we can achieve much more spectacular progress in speed than in space. Therefore, following a well-established tradition of algorithm textbooks, we primarily concentrate on time efficiency. For example, it takes longer to sort larger arrays, multiply larger matrices, and so on. There are situations, where the choice of a parameter indicating an input size does matter. The choice of an appropriate size metric can be influenced by operations of the algorithm in question. If the algorithm examines individual characters of its input, then we should measure the size by the number of characters; if it works by processing words, we should count their number in the input. We should make a special note about measuring the size of inputs for algorithms involving properties of numbers. This metric usually gives a better idea about the efficiency of algorithms in question. The thing to do is to identify the most important operation of the algorithm, called the basic operation, the operation contributing the most to the total running time, and compute the number of times the basic operation is executed. For example, most sorting algorithms work by comparing elements of a list being sorted with each other; for such algorithms, the basic operation is a key comparison. As another example, algorithms for matrix multiplication and polynomial evaluation require two arithmetic operations: Prepared by Harivinod N. Then we can estimate the running time T_n of a program implementing this algorithm on that computer by the formula: Values of several functions important for analysis of algorithms Algorithms that require an exponential number of operations are practical for solving only problems of very small sizes. The worst-case efficiency of an algorithm is its efficiency for the worst-case input of size n , for which the algorithm runs the longest among all possible inputs of that size. Consider the algorithm for sequential search. Prepared by Harivinod N Page 1. Introduction The running time of above algorithm can be quite different for the same list size n . In the worst case, when there are no matching elements or the first matching element happens to be the last one on the list, the algorithm makes the largest number of key comparisons among all possible inputs of size n : Thus it guarantees that for any instance of size n , the running time will not exceed $C_{\text{worst}} n$, its running time on the worst-case inputs. The best-case efficiency of an algorithm is its efficiency for or the best-case input of size n , for which the algorithm runs the fastest among all possible inputs of that size. We determine the kind of inputs for which the count C_n will be the smallest among all possible inputs of size n . The analysis of the best-case efficiency is not nearly as important as that of the worst-case efficiency. This information is provided by average-case efficiency. Let us consider again sequential search. We can find the average number of key comparisons $C_{\text{avg}} n$ as follows. In the case of an unsuccessful search, the number of comparisons is n with the probability of such a search being $1-p$. Therefore, Investigation of the average-case efficiency is considerably more difficult than investigation of the worst-case and best-case efficiencies. But there are many important algorithms for which the average case efficiency is much better than the overly pessimistic worst-case efficiency would lead us to believe. Space efficiency is measured by counting the number of extra memory units consumed by the algorithm. The efficiencies of some algorithms may differ significantly for inputs of the same size. For such algorithms, we need to

distinguish between the worst-case, average-case, and best-case efficiencies. Performance Analysis 2. This includes memory space for codes, variables, constants and so on. A variable part that depends on the input, output and recursion stack. Consider following algorithm abc Here fixed component depends on the size of a, b and c. Let us consider the algorithm to find sum of array. For the algorithm given here the problem instances are characterized by n, the number of elements to be summed. The space needed by a[] depends on n. This is the sum of the time taken to execute all instructions in the program. Exact estimation runtime is a complex task, as the number of instructions executed is dependent on the input data. Also different instructions will take different time to execute. So for the estimation of the time complexity we count only the number of program steps. A program step is loosely defined as syntactically or semantically meaningful segment of the program that has an execution time that is independent of instance characteristics. We can determine the steps needed by a program to solve a particular problem instance in two ways. In the first method we introduce a new variable count to the program which is initialized to zero. We also introduce statements to increment count by an appropriate amount into the program. So when each original program executes, the count also incremented by the step count. Consider the algorithm sum. After the introduction of the count the program will be as follows. The second method to determine the step count of an algorithm is to build a table in which we list the total number of steps contributed by each statement. An example is shown below. Prepared by Harivinod N.

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Since multiplications are more expensive than additions, let us count the cost of multiplications only. Here, we have to keep track of the lengths of the entries of the matrix. So the running time of computing F_n using Method 3 is dependent on the multiplication algorithm. Well, multiplication is multiplication – what can we do about it? Before that let us summarize what we know about it. Multiplying two n digit numbers using the add-and-shift method takes $O(n^2)$ steps where each step involves multiplying two single digits bits in the case of binary representation, and generating and managing carries. For binary representation this takes $O(n)$ for multiplying with each bit and finally n shifted summands are added – the whole process takes $O(n^2)$ steps. Using such a method of multiplication implies that we cannot do better than n^2 steps to compute F_n . For any significant asymptotically better improvement, we must find a way to multiply faster. What is maximum size of the numbers involved in subtraction? The running time is roughly $O(n)$. It is possible to multiply much faster using a generalization of the above method in $O(n \log n \log \log n)$ by a method of Schonage and Strassen. However it is quite involved as it uses Discrete Fourier Transform computation over modulo integer rings and has fairly large constants that neutralize the advantage of the asymptotic improvement unless the numbers are a few thousand bits long. Despite architectural variations, the assembly level language support is very similar – the major difference being in the number of registers and the word length of the machine. But these parameters are also in a restricted range of a factor of two, and hence asymptotically in the same ball park. In summary, think about any computer as a machine that supports a basic instruction set consisting of arithmetic and logical operations and memory accesses including indirect addressing. We will avoid cumbersome details of the exact instruction set and assume realistically that any instruction of one machine can be simulated using a constant number of available instruction of another machine. Since analysis of algorithms involves counting the number of operations and not the exact timings which could differ by an order of magnitude, the above simplification is justified. The careful reader would have noticed that during our detailed analysis of Method 3 in the previous sections, we were not simply counting the number of arithmetic operations but actually the number of bit-level operations. Therefore the cost of a multiplication or addition was not unity but proportional to the length of the input. Had we only counted the number of multiplications for computing x_n , that would only be $O(\log n)$. This would indeed be the analysis in a uniform cost model where only the number of arithmetic also logical operations are counted and does not depend on the length of the operands. A very common use of this model is for comparison-based problems like sorting, selection, merging, and many data-structure operations. For these problems, we often count only the number of comparisons not even other arithmetic operations without bothering about the length of the operands involved. In other words, we implicitly assume $O(1)$ cost for any comparison. This is not considered unreasonable since the size of the numbers involved in sorting do not increase during the course of the algorithm for majority of the commonly known sorting problems. On the other hand consider the following problem of repeated squaring n times starting with 2. The resultant is a number 2^{2^n} which requires 2^n bits to be represented. It will be very unreasonable to assume that a number that is exponentially long can be written out or even stored in $O(n)$ time. Therefore the uniform cost model will not reflect any realistic setting for this problem. On the other extreme is the logarithmic cost model where the cost of an operation is proportional to length of the operands. This is very consistent with the physical world and also has close relation with the Turing Machine model which is a favorite of complexity theorists. Our analysis in the previous sections is actually done with this model in mind. It is not only the arithmetic operations but also the cost of memory access is proportional to the length of the address and the operand. We assume that for an input of size n , any operation involving operands of size $\log n$ takes $O(1)$ steps. This is justified as follows. All microprocessor chips have specialized hardware circuits for arithmetic operations like multiplication, addition, division etc. The reason that $\log n$ is a natural choice for a word is that, even to address an input size n , you require $\log n$

bits of address space. We will also use this model, popularly known as Random Access Machine or RAM in short except for problems that deal with numbers as inputs like multiplication in the previous section where we will invoke the log cost model. In the beginning, it is desirable that for any algorithm, you get an estimate of the maximum size of the numbers to ensure that operands do not exceed $\log n$ so that it is safe to use the RAM model. There is clear trade-off between the simplicity and the fidelity achieved by an abstract model. One of the obvious and sometimes serious drawback of the RAM model is the assumption of unbounded number of registers since the memory access cost is uniform. In reality, there is a memory hierarchy comprising of registers, several levels of cache, main memory and finally the disks. We incur a higher access cost as we go from registers towards the disk and for technological reason, the size of the faster memory is limited. There could be a disparity of between the fastest and the slowest memory which makes the RAM model somewhat suspect for larger input sizes. This has been redressed by the external memory model. Given the rather high cost of a disk access compared to any CPU operation, this model actually ignores all other costs and counts only the number of disk accesses. The disk is accessed as contiguous memory locations called blocks. The blocks have a fixed size B and the simplest model is parameterized by B and the size of the faster memory M . In this two level model, the algorithms are only charged for transferring a block between the internal and external memory and all other computation is free. As the model becomes more complicated, designing algorithms also becomes more challenging and often more laborious. At the most intuitive level it symbolises what can be achieved by cooperation among individuals in terms of expediting an activity. It is not in terms of division of labor or specialisation, but actually assuming similar capabilities. Putting more labourers clearly speeds up the construction and similarly using more than one processor is likely to speed up computation. Ideally, by using p processors we would like to obtain a p -fold speed up over the conventional algorithms; however the principle of decreasing marginal utility shows up. One of the intuitive reasons for this that with more processors as with more individuals, the communication requirements tend to dominate after a while. But more surprisingly, there are algorithmic constraints that pose serious limitations to our objective of obtaining proportional speed-up. Here p processors are connected to a shared memory and the communication happens through reading and writing in a globally shared memory. It is left to the algorithm designer to avoid read and write conflicts. It is further assumed that all operations are synchronized globally and there is no cost of synchronization. In this model, there is no extra overhead for communication as it is charged in the same way as a local memory access. Even in this model, it has been shown that it is not always possible to obtain ideal speed up. As an example consider the elementary problem of finding the minimum of n elements. It has been proved that with n processors, the time parallel time is at least $\log \log n$. For certain problems, like depth first search of graphs, it is known that even if we use any polynomial number of processors, we cannot obtain polylogarithmic time! So, clearly not all problems can be parallelized effectively. A more realistic parallel model is the interconnection network model that has an underlying communication network, usually a regular topology like a two-dimensional mesh, hypercube etc. These can be embedded into VLSI chips and can be scaled according to our needs. To implement any parallel algorithm, we have to design efficient schemes for data routing. A very common model of parallel computation is a hardware circuit comprising of basic logic gates. The signals are transmitted in parallel through different paths and the output is a function of the input. The size of the circuit is the number of gates and the parallel time is usually measured in terms of the maximum path length Δ from any input gate to the output gate each gate contributes to a unit delay. Those familiar with circuits for addition, comparison can analyse them in this framework. The carry-save adder is a low-depth circuit that adds two n -bit numbers in about $O(\log n)$ steps which is much faster than a sequential circuit that adds one bit at a time taking n steps. One of the most fascinating developments is the Quantum Model which is inherently parallel but it is also fundamentally different from the previous models. A breakthrough result in recent years is a polynomial time algorithm for factorization which forms the basis of many cryptographic protocols in the conventional model. Biological Computing models is a very active area of research where scientists are trying to assemble a machine out of DNA strands. It has potentially many advantages over silicon based devices and is inherently parallel.

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Note that if a set is represented by a list, depending on the application at hand, it might be worth maintaining the list in a sorted order. Dictionary: In computing, the operations we need to perform for a set or a multiset most often are searching for a given item, adding a new item, and deleting an item from the collection.